A TWO STAGE EQUALIZER FOR TRELLIS CODED SYSTEMS

CROSS-REFERENCE TO RELATED APPLICATIONS

The invention disclosed in this patent application is related to the invention disclosed in United States Patent Application Serial Number [Attorney Docket No. PHIL06-01408] by M. Ghosh et al. entitled "System and Method for Reducing Error Propagation in a Decision Feedback Equalizer of an ATSC VSB Receiver" filed concurrently with this patent application. The invention disclosed in this patent application is also related to the invention disclosed in United States Patent Application Serial Number [Attorney Docket No. PHIL06-01720] by K. Wittig et al. entitled "Generation of Decision Feedback Equalizer Data Using Trellis Decoder Traceback Output in an ATSC HDTV Receiver" filed concurrently with this patent application. The related patent applications are commonly assigned to the assignee of the present invention. The disclosures of the related patent applications are hereby incorporated by reference in the present patent application as if fully set forth herein.

TECHNICAL FIELD OF THE INVENTION

The present invention is directed, in general, to digital communication devices and, more specifically, to a system and method for operating a two stage equalizer in trellis coded systems to reduce errors by utilizing symbol stream information from a trellis decoder to provide estimates for a decision feedback equalizer.

BACKGROUND OF THE INVENTION

The Digital High Definition Television (HDTV) Grand Alliance (Grand Alliance) is a group of television manufacturing and research organizations in the television industry. After years of cooperative effort the Grand Alliance developed and proposed a standard for digital HDTV systems. The Grand Alliance standard has been adopted (with a few changes) by the Federal Communication Commission (FCC) as an official broadcasting standard for HDTV. The standard is known as the Advanced Television Systems Committee Digital Television Standard (the "ATSC Standard").

The ATSC Standard for HDTV transmission over terrestrial broadcast channels uses a signal that consists of a sequence of twelve (12) independent time-multiplexed trellis-coded data streams

modulated as an eight (8) level vestigial sideband (VSB) symbol stream with a rate of 10.76 MHz. This signal is converted to a six (6) MHz frequency band that corresponds to a standard VHF or UHF terrestrial television channel, over which the signal is then broadcast.

The ATSC Standard calls for two (2) bit data symbols of the HDTV signal to be trellis encoded in accordance with an eight (8) level (i.e., a three (3) bit) one dimensional constellation. One bit of each data symbol is pre-coded, and the other is subjected to a 1/2 encoding rate that produces two coded bits in accordance with a four (4) state trellis code. For purposes of interleaving, twelve (12) identical encoders and pre-coders operate successively on every twelve successive data symbols. Symbols 0, 12, 24, 36, . . . are encoded as one series. Symbols 1, 13, 25, 37, . . . as a second series. Symbols 2, 14, 26, 38, . . . as a third series. And so on for a total of twelve (12) series. Therefore, the ATSC Standard requires twelve (12) trellis decoders in the HDTV receiver for the twelve (12) series of time division interleaved data symbols in the signal. Each trellis decoder in the HDTV receiver decodes every twelfth (12th) data symbol in the stream of coded data symbols.

In an ATSC Standard receiver trellis decoders are used to retrieve the original digital data that was trellis encoded just

before being converted to 8-VSB symbols, modulated and broadcast. The use of trellis coding provides an improvement in the signal to noise ratio of the received signal, and the time multiplexing of twelve (12) independent streams reduces the possibility of co-channel interference from an analog NTSC broadcast signal residing on the same frequency. The abbreviation NTSC stands for National Television Standards Committee.

Each of the trellis decoders for the four (4) state trellis code operates in accordance with the well-known Viterbi decoding algorithm. Each of the decoders comprises a branch metric generator unit, an add-compare-select unit, and a path-memory unit. See, for example, "Trellis-coded Modulation With Redundant Signal Set, Part I, Introduction; Part II, State of the Art," by G. Ungerboeck, IEEE Communications Magazine, Vol. 25, pp. 5-21, February 1987.

In addition to being corrupted by noise, the transmitted signal is also subject to deterministic channel distortions and distortions caused by multipath interference. Consequently, an adaptive channel equalizer is generally used in front of the trellis decoders to compensate for these effects. The goal is to create a symbol stream that resembles, as much as possible, the symbol stream that was created by the twelve (12) trellis encoders at the transmitter.

One commonly used equalizer architecture makes use of a second equalizer known as a decision feedback equalizer (DFE). In this architecture, a conventional, or forward equalizer (FE) is supplemented by a DFE. The input to the DFE is an estimate of the original transmitted value of the current output symbol of the complete equalizer (FE and DFE). The output of the decision feedback equalizer (DFE) is subsequently added to the output of the forward equalizer (FE) to generate the output symbol. In a typical implementation, this estimate of the output symbol is obtained by simply "slicing" the equalizer output. The term "slicing" refers to the process of taking the allowed symbol value (of the eight (8) levels specified by the 8-VSB ATSC Standard) that is nearest to that of the actual output. Using the "sliced" symbols in a decision feedback equalizer (DFE) gives a near optimum error rate performance with low complexity. This approach, however, can suffer from error propagation caused by slicing errors. Because the typical symbol error rate after the equalizer for the HDTV signal can be up to twenty percent (20%), this can be a serious problem if the number of DFE filter taps is large.

After the equalizer, the HDTV signal is decoded in a trellis decoder that uses the Viterbi algorithm to decode the symbol stream based on the 1/2 rate trellis coding performed in the transmitter. As previously mentioned, the ATSC Standard specifies that twelve

(12) trellis encoders and decoders are used in parallel in a time multiplexed fashion. Trellis decoding is then followed by byte de-interleaving and Reed Solomon decoding to further correct transmission errors in the signal.

There is a need in the art for a system and method that will reduce error propagation in a decision feedback equalizer used in trellis coded systems in general and in ATSC VSB receivers in particular.

SUMMARY OF THE INVENTION

To address the above-discussed deficiencies of the prior art, the system and method of the present invention reduces error propagation in a decision feedback equalizer in an ATSC VSB receiver by utilizing symbol stream information from a trellis decoder. The present invention provides an improved two stage trellis coded system for reducing error propagation.

The output symbols from the adaptive channel equalizer are input to a trellis decoder. The trellis decoder uses "soft" decision making to determine the most likely symbol values that were originally transmitted as opposed to "hard" decision making such as "slicing." Soft decision methods take into account the restricted set of values that the symbol following a symbol having a given value is permitted to assume by the trellis encoder. Soft decision methods use this additional information to obtain a more reliable estimate of the actual value than can be obtained by hard decision methods that only consider the current symbol.

The system and method of the present invention uses information from the trellis decoder to generate an estimate of the equalizer output that serves as the input to the decision feedback equalizer (DFE). The system and method of the present invention essentially incorporates a trellis decoder into the equalizer to provide the estimates of the actual symbol values that are needed

by the decision feedback equalizer (DFE). Due to the nature of the Viterbi algorithm, which performs a trace-back over a path consisting of previously received symbols and having a specified length, an estimate is provided not only for the current symbol, but for all of the previous symbols that constitute this path. Since the Viterbi algorithm is known to provide the best estimate of the value of the transmitted symbol data under conditions of Gaussian channel noise, such an approach results in more reliable data being input to the decision feedback equalizer (DFE) than was possible using simple slicing of the equalizer output. This in turn results in better equalizer performance, and therefore in more reliable data being input to the trellis decoder.

A related method uses a second equalizer, whose decision feedback equalizer (DFE) input is the output of this trellis decoder as well as the training sequence for the equalizer adaptation. Since the trellis decoder provides an optimum estimate of the symbol data, its output can be reliably used as a training sequence even though it is only an estimate and does not constitute a priori knowledge of the transmitted data, as is the case with a known training sequence.

The ATSC trellis decoder system consisting of twelve (12) time multiplexed Viterbi decoders is fairly complicated and requires a substantial amount of hardware to implement. Also, an adaptive

channel equalizer is, in general, the most complicated component of a digital data demodulator in terms of the amount of hardware required to implement it. It is also therefore the most expensive component.

A trellis decoder in accordance with the principles of the present invention is adapted for decoding each of a plurality of interleaved series of data symbols, each series having been trellis encoded in accordance with a multi-level constellation of permissible trellis code values. Such a decoder comprises a branch metric generator for deriving for each series the branch metrics of each of the trellis states as successively determined for successive data symbols in such series. The branch metric and trellis state information is supplied to an add-compare-select (ACS) unit which determines the best metric paths which are successively updated for each series in accordance with successively received data symbols in each series. The decoder also comprises successive path memory stages, the outputs of each stage being the inputs of the next succeeding stage, each stage receiving from its predecessor and storing a pointer identifying the path having the best metric through the trellis for the previously received data symbol in each of said series, the first stage receiving from the ACS unit and storing a pointer identifying the path having the best metric through the trellis for currently

received data symbols in each of said series. The final memory stage thereby will have stored therein a pointer for the trellis states corresponding to the earliest of the data symbols in each of the series of stored trellis states in all of the path memory stages, from which trellis states the fully decoded value of said earliest data symbol is indicated.

According to one feature of the present invention, the decoder makes use of the fact that for certain trellis codes, including the four (4) state code of the ATSC Standard, the trellis states can be divided into a plurality of distinct groups such that the states existing at any time in a given group can only have resulted from preceding trellis states within that same group. In addition, any existing state can only have resulted from a small number of possible predecessor states. Codes having both those characteristics are called "well-defined" codes. In particular, for a larger number of well-defined codes, the number of possible predecessor states depends on the number of trellis coded input bits. That number is one in the ATSC Standard and in the majority of trellis codes presently in use, and hence the number of possible predecessor states in those codes is only two. The four (4) state trellis code of the ATSC Standard is an example of a well-defined code, whereby it is possible to provide two ACS sub-units to respectively derive best metric path data for only the two trellis

states in respective ones of first and second groups. Each such ACS sub-unit is thereby much simpler in design and operation that would be a single ACS unit for both of said groups. This approach can be taken for well-defined codes of any number of states. For example, with an eight (8) state code there may be four groups of two (2) states each, and four ACS units would each handle one such group.

According to a further feature of the present invention, the path memory unit is constituted by successive storage sections in a single random access memory (RAM), as the simplification of the path memory unit reduces the required input/output by a similar amount.

Another feature of "well-defined" codes that is exploited in the present invention is the simplification of the path memory required for each state of the trellis code. Since any existing state could have been reached from only a small number "s" of possible predecessor states, it is not necessary to store a pointer to all possible predecessor states. Instead, a pointer is stored which distinguishes between the small set of possible predecessor states. This requires only a number of memory elements at least equal to $\log_2 s$. Use is made of the information identifying the particular sets to clearly determine the pointer to the previous state. This implies that a small penalty may be paid in terms of

extra logic required to determine the pointer to the previous state. However, the second condition of the well-defined code, namely that of distinct groups of code states such that those existing at any time in a given group can only have resulted from previous states in that same group, ensures that the extra logic is actually simpler than would be required to implement a conventional path memory unit. Such simplification can achieve a reduction by a factor of two in regard to the memory required for the four (4) state ATSC code, and reduction by a factor of three in the case of an eight (8) state code. The saving in memory capacity is therefore substantial.

A further feature of the present invention which is specific to the four (4) state ATSC code is that the path memory logic required for selection of a pointer among possible predecessor states at every stage is simplified so that the propagation delay in the combinatorial logic required for computation of each traceback portion of the overall path is reduced by a factor of two. This has significant advantages in regard to the speed at which the trellis decoder can be operated and results in fewer logic elements.

An HDTV receiver in accordance with the present invention is adapted to receive a digital HDTV signal having successive data frames each of which includes successive data segments, each

segment including successive data symbols, the data symbols being interleaved to form a plurality of data streams which are each trellis encoded in accordance with a code having a multi-level constellation of permissible code values. Such receiver includes a trellis decoder as described above.

It is an object of the present invention to provide a system and method for reducing errors in a decision feedback equalizer in an ATSC VSB receiver by utilizing symbol stream information from a trellis decoder.

It is another object of the present invention to provide a system and method for decoding "best guess" values for symbols in a trellis decoder.

It is also an object of the present invention to provide a system and method that sends "best guess" values for symbols from a trellis decoder to decision feedback equalizer in an ATSC VSB receiver.

It is another object of the present invention to provide a system and method for performing channel equalization in an ATSC VSB receiver with a decision feedback equalizer that uses "best guess" values for symbols from a trellis decoder.

It is also an object of the present invention to provide a system and method for reducing errors in a decision feedback equalizer in an ATSC VSB receiver by utilizing a first combination

of a first equalizer unit and a first trellis decoder and a second combination of a second equalizer unit and a second trellis decoder.

The foregoing has outlined rather broadly the features and technical advantages of the present invention so that those skilled in the art may better understand the detailed description of the invention that follows. Additional features and advantages of the invention will be described hereinafter that form the subject of the claims of the invention. Those skilled in the art should appreciate that they may readily use the conception and the specific embodiment disclosed as a basis for modifying or designing other structures for carrying out the same purposes of the present invention. Those skilled in the art should also realize that such equivalent constructions do not depart from the spirit and scope of the invention in its broadest form.

Before undertaking the Detailed Description of the Invention, it may be advantageous to set forth definitions of certain words and phrases used throughout this patent document: the terms "include" and "comprise" and derivatives thereof, mean inclusion without limitation; the term "or," is inclusive, meaning and/or; the phrases "associated with" and "associated therewith," as well as derivatives thereof, may mean to include, be included within, interconnect with, contain, be contained within, connect to or

with, couple to or with, be communicable with, cooperate with, interleave, juxtapose, be proximate to, be bound to or with, have, have a property of, or the like; and the term "controller," "processor," or "apparatus" means any device, system or part thereof that controls at least one operation, such a device may be implemented in hardware, firmware or software, or some combination of at least two of the same. It should be noted that the functionality associated with any particular controller may be centralized or distributed, whether locally or remotely. In particular, a controller may comprise one or more data processors, and associated input/output devices and memory, that execute one or more application programs and/or an operating system program. Definitions for certain words and phrases are provided throughout this patent document. Those of ordinary skill in the art should understand that in many, if not most instances, such definitions apply to prior, as well as future uses of such defined words and phrases.

BRIEF DESCRIPTION OF THE DRAWINGS

For a more complete understanding of the present invention, and the advantages thereof, reference is now made to the following descriptions taken in conjunction with the accompanying drawings, wherein like numbers designate like objects, and in which:

FIGURE 1 illustrates a block diagram of an exemplary high definition television (HDTV) transmitter;

FIGURE 2 illustrates a block diagram of an exemplary high definition television (HDTV) receiver;

FIGURE 3 illustrates s a block diagram of a trellis encoder comprising twelve (12) parallel trellis encoder and pre-coder units for twelve groups of interleaved data symbols;

FIGURE 4 illustrates a block diagram of one exemplary trellis encoder and pre-coder unit (one of the twelve (12) such units shown in FIGURE 3) and an eight (8) level symbol mapper;

FIGURE 4A illustrates the four subsets a, b, c, d of the constellation code values R;

FIGURES 5A, 5B, and 5C illustrate respectively a trellis diagram, a state diagram, and a trellis code value tabulation applicable to the exemplary ATSC trellis encoder shown in FIGURE 4;

FIGURE 6 illustrates a block diagram of an exemplary ATSC trellis decoder;

FIGURE 7 illustrates a block diagram of an adaptive channel equalizer comprising a forward equalizer (FE) filter and a decision feedback equalizer (DFE) filter;

FIGURE 8 illustrates a block diagram of an adaptive finite impulse response (FIR) filter for use in an adaptive channel equalizer;

FIGURE 9 illustrates a block diagram of the present invention showing the connection of a forward equalizer (FE) filter to a trellis decoder and the connection of the trellis decoder to a decision feedback equalizer (DFE) filter;

FIGURE 10 illustrates a block diagram of the present invention showing in more detail the connection of the trellis decoder to the decision feedback equalizer (DFE) filter;

FIGURE 11 illustrates a block diagram showing a combination of a first equalizer and a first trellis decoder and a combination of a second equalizer and a second trellis decoder;

FIGURE 12 illustrates a flow diagram showing an advantageous embodiment of the method of the present invention;

FIGURE 13 illustrates a block diagram showing an advantageous embodiment of the two stage equalizer of the present invention;

FIGURE 14 illustrates a block diagram showing an advantageous embodiment of the two stage equalizer of the present invention in a less complex form; and

FIGURE 15 illustrates a block diagram showing an advantageous embodiment of one implementation the two stage equalizer of the present invention.

DETAILED DESCRIPTION OF THE INVENTION

FIGURES 1 through 15, discussed below, and the various embodiments used to describe the principles of the present invention in this patent document are by way of illustration only and should not be construed in any way to limit the scope of the invention. In the description of the exemplary embodiment that follows, the present invention is integrated into, or is used in connection with, a high definition television system. Those skilled in the art will recognize that the exemplary embodiment of the present invention may easily be modified for use in other similar types of systems for modulating and demodulating digital data.

FIGURE 1 illustrates a block diagram of an exemplary high definition television (HDTV) transmitter 100. MPEG compatible data packets are encoded for forward error correction (FEC) by a Reed Solomon (RS) encoder 110. The data packets in successive segments of each data field are then interleaved by data interleaver 120, and the interleaved data packets are then further interleaved and encoded by trellis encoder unit 130. Trellis encoder unit 130 produces a stream of data symbols representing three (3) bits for each symbol. One of the three bits is pre-coded and the other two bits are produced by a four (4) state trellis encoding.

As will be more fully discussed, trellis encoder unit 130 comprises twelve (12) parallel trellis encoder and pre-coder units

to provide twelve interleaved coded data sequences. The encoded three (3) bits of each trellis encoder and pre-coder unit are combined with field and segment synchronization bit sequences in multiplexer 140. A pilot signal is inserted by pilot insertion unit 150. The data stream is then subjected to vestigial sideband (VSB) suppressed carrier eight (8) level modulation by VSB modulator 160. The data stream is then finally up-converted to a radio frequency by radio frequency (RF) by converter 170.

FIGURE 2 illustrates a block diagram of an exemplary high definition television (HDTV) receiver 200. The received RF signal is down-converted to an intermediate frequency (IF) by tuner 210. The signal is then filtered and converted to digital form by IF filter and detector 220. The detected signal is then in the form of a stream of data symbols that each signify a level in an eight (8) level constellation. The signal is then filtered by NTSC rejection filter 230 and subjected to equalization and phase tracking by equalizer and phase tracker unit 240. The recovered encoded data symbols are then subjected to trellis decoding by trellis decoder unit 250. The decoded data symbols are then further de-interleaved by data de-interleaver 260. The data symbols are then subjected to Reed-Solomon decoding by Reed Solomon decoder 270. This recovers the MPEG compatible data packets transmitted by transmitter 100.

FIGURE 3 illustrates how the interleaved data from data interleaver 120 are further interleaved during the trellis encoding process. Demultiplexer 310 of trellis encoder unit 130 distributes each successive series of twelve (12) data symbols among twelve (12) successive trellis encoder and pre-coder units 320A, 320B, 320C, ..., 320K, and 320L. The encoded outputs of the twelve (12) successive trellis encoder and pre-coder units are then time division multiplexed by multiplexer 330 to form a single data stream. The single data stream is sent to eight (8) level symbol mapper 430 of trellis encoder unit 130.

FIGURE 4 illustrates a block diagram of an exemplary trellis encoder and pre-coder unit 320A and its output to eight (8) level symbol mapper 430. Not shown in FIGURE 4 is multiplexer 330 that couples trellis encoder and pre-coder unit 320A to eight (8) level symbol mapper 430. Trellis encoder and pre-coder unit 320A comprises pre-coder 410 and trellis encoder 420. Each data symbol to be encoded comprises two bits, X_1 and X_2. Bit X_2 is pre-coded by pre-coder 410 which comprises a one bit register 440 to derive pre-coded bit Y_2. Bit Y_2 is not altered further by trellis encoder 420 and is output as bit Z_2.

The other input bit, X_1, does not pass through pre-coder 410. Bit X_1 (also denoted bit Y_1) does pass through trellis encoder 420. Trellis encoder 420 encodes bit X_1 in accordance with a rate 1/2

trellis code utilizing one bit data registers 450 and 460. The result is output as bit Z_0 and bit Z_1. Therefore, three bits (i.e., bit Z_0, bit Z_1, and bit Z_2) are output by trellis encoder 420 to eight (8) level symbol mapper 430. Eight (8) level symbol mapper 430 converts the three bits to a value R in an eight (8) level constellation of permissible code values. The permissible code values for R are -7, -5, -3, -1, +1, +3, +5, and +7. These values correspond with the three bit combinations shown in eight (8) level symbol mapper 430.

The above described process is carried out for each of the twelve interleaved series of data symbols. Eight (8) level symbol mapper 430 comprises a look-up table for selecting the correct R code value for a given set of three input bits. It is seen that the eight (8) level constellation has four possible subsets of bits Z_1 and Z_0, each subset having dual possible constellation values depending whether the pre-coded bit Z_2 is a zero ("0") or a one ("1"). Those subsets and the corresponding constellation values are shown in FIGURE 4A. Further details of the encoder and its operation are given in Appendix D of the ATSC Standard. For a basic description of the logic operations involved in trellis encoding and decoding, refer to "Principles of Communication Systems," by H. Taub et al., 2nd edition, pp. 562-571, McGraw Hill, New York, 1986.

To understand how a single trellis decoder can decode twelve interleaved series of data symbols obtained from an HDTV signal, refer to the four (4) state trellis diagram in FIGURE 5A. FIGURE 5A and the corresponding state diagram in FIGURE 5B ignore pre-coder 410 in FIGURE 4 which supplements trellis encoder 420, because the pre-coding has a very simple inverse that is described in the ATSC Standard. The trellis diagram in FIGURE 5A relates to the successive values of uncoded bit X_1 in FIGURE 4 in successive symbol periods. The two active registers, 450 and 460, have bit values which during any symbol period determine the four (4) possible code states "00", "01", "10", "11". If the next X_1 bit is a zero ("0"), the present code state will change to the succeeding state indicated by the solid line leaving the present state, and if the X_1 bit is a one ("1"), the present state will change to the succeeding state indicated by a dashed line leaving the present state. The output of the decoder is the Z_1, Z_0 subset indicated in each case at the end of the state change line.

Thus, for example, if the present code state D_1, D_0 is "01" and the next X_1 bit is a zero ("0"), then the next code state D_1, D_0 will be "10" and the Z_1, Z_0 output subset of the decoder will be "01". The pre-coded bit Z_2 received by the decoder serves, as described above, to distinguish between the two possible outputs that can result from each transition between trellis states. The

possible coded output subsets Z_1, Z_0 resulting from uncoded input bit X_1, and the possible transitions between the present (PS) and next (NS) code states D_1, D_0 are shown in the table in FIGURE 5C. For any given code state (i.e., the values D_1, D_0 of the bits in registers 450 and 460) only two possible transitions can be produced by the input bit X_1, depending on whether it is a zero ("0") or a one ("1"). As seen in FIGURE 5A, given a particular initial code state D_1, D_0 (which is typically "00") a specific sequence of input bits X_1 will select a particular path through the trellis diagram. There are four possible values of output Z_1, Z_0, constituting the above-mentioned four subsets a, b, c and d shown in FIGURE 4A and also marked on the state transition lines in FIGURE 5A. The code states and possible transitions are also shown in the state diagram in FIGURE 5B. Each transition line therein is marked with

$$(X_1) / (Z_1 Z_0) \qquad (1)$$

where X_1 is the input bit value and Z_1 Z_0 is the resulting coded output subset.

A trellis decoder must reconstruct a transmitted sequence of data symbols from a received noise-corrupted encoded version of the transmitted sequence. The first step is to identify the code subset signified by a received symbol. Selection of the nearest of the two constellation points corresponding to that subset is then

made by passing the received symbol through a detector having a threshold set at a level exactly halfway between the two constellation points. In this way an accurate determination can be made as to the encoded symbol that was transmitted.

To evaluate a received sequence of coded symbols, the paths through the trellis diagram must be accurately determined. Essentially, from among all possible paths that exist through the trellis diagram the one that comes "closest" to the actual received symbol sequence must be selected. While this might initially seem to require an inordinate number of calculations, a significant simplification is achieved by making use of the Viterbi algorithm. This is described in the text "Principles of Digital Communication and Coding," by Viterbi et al., McGraw Hill, New York, 1979. According to the Viterbi algorithm, the number of surviving paths at every stage of the trellis decoding process is equal to the total number of trellis states of the trellis code. That is, only one surviving path, consisting of the closest match to the actually received sequence, is continued to the following state of the trellis. This is based on the observation that the match between a received sequence and a specific branch in the trellis can be described in terms of a metric, and the branch metrics are additive. The cumulative metric of a path is called the path metric, and is the sum of all of the branch metrics of that path.

Each branch metric corresponds to the difference between the output corresponding to a specific branch within the trellis diagram in FIGURE 5A and the actual received symbol value corresponding to that branch.

Accordingly, a Viterbi decoder requires a branch metric generator (BMG) unit which calculates a distance ("branch metric") in each bit period between a received bit value and the bit values of all the trellis paths leading up to the code state existing during that bit period. The branch metrics are supplied to an add-compare-select (ACS) unit that maintains the accumulated path metrics, one for each of the code states. The ACS unit also determines, for each successive new code state, the path having the minimum (i.e., best) path metric to that state and this path is selected and stored in the form of a pointer in a path memory unit (PMU) defining the new path to that code state. That constitutes the most likely (survivor) trellis path to that code state. Finally, a traceback unit traces back along the accumulated survivor paths to thereby determine the sequence of bits constituting the most likely transmitted data sequence. The number of traceback steps is called the decoding depth, and the oldest bit on the traceback path is output as a decoded bit. The traceback unit must therefore store the aforesaid number of most recent traceback steps, which are in the form of pointers or "decision

vectors."

In accordance with the aforesaid description, for every destination state (on the right side of FIGURE 5A) the ACS unit must determine the appropriate branch metric to add to the already accumulated path metric going back to the preceding states that end in that destination state, and then select as the surviving path the one having the smallest resultant path metric.

Note that a description of the state transitions which result in the surviving path must be stored following each successive received symbol in a sequence. This consists of the accumulated path metric leading up to the present state, and also the precise sequence of transitions between all previous states in order to arrive at the present state. Clearly, it is impossible to store all possible transitions leading to a given state. A sub-optimal solution is to store all transitions up to a specified number of states preceding the present state. The trellis state transition corresponding to the pointer stored in the path memory unit (PMU) corresponding to the earliest branch which has resulted in the best metric among all the states existing at the current transition is then used to determine the decoded symbol. Such decoded symbol is described by identifying the pre-coded bit and also which of the subsets a, b, c, or d correspond to the encoded bit as described above. This trellis decoding strategy is well known and is

described in the above-referenced textbook by Viterbi and also in a technical paper entitled "A Programmable Parallel Processor Architecture For A Viterbi Detector," by H. Lou et al., Globecom, 1990.

The transition history of each surviving path metric is stored in the path memory unit (PMU). A simplified implementation of the PMU which separates memory-based functions from logic functions thereof is described in a technical paper entitled "Memory Management in a Viterbi Decoder," by C. M. Rader, IEEE Trans. Comms., Vol. Com-29, No. 9, September 1981. Basically, the idea is to compute the past state transition sequence best corresponding to the present state. What then needs to be stored for every state is a selective pointer to the best corresponding previous state. These pointers can then be sequentially used to identify the selected branch at the earliest stage of the PMU and consequently the initial decoded symbol in the complete sequence.

FIGURE 6 illustrates a block diagram of an exemplary ATSC trellis decoder 250. Trellis decoder unit 250 comprises a branch metric generator (BMG) unit 610, an add-compare-select (ACS) unit 620, a path memory unit (PMU) 630, a traceback unit 640, and a subset bit delay unit 650. Trellis decoder unit 250 also comprises a subset bit multiplexer 670 and an output decode logic unit 680. The terms "met_a", "met_b", "met_c", and "met_d" in branch metric

generator (BMG) unit 610 refer to a branch metric for the current input symbol corresponding to each subset (a, b, c, d). The terms "sub_a", "sub_b", "sub_c", and "sub_d" in branch metric generator (BMG) unit 610 refer to a subset (uncoded) bit for the current input symbol corresponding to each subset (a, b, c, d). The terms "svr0", "svr1", "svr2", and "svr3" in add-compare-select (ACS) unit 620 refer to a pointer to the previous trellis state for the survivor path corresponding to each possible current state. The term "SVR" in add-compare-select (ACS) unit 620 refers to the survivor path with the lowest cumulative metric. The pointers "svr0", "svr1", "svr2", and "svr3" to the previous state in each survivor path may be implemented using one (1) or two (2) bits each.

It is understood the component elements of trellis decoder unit 250 described herein are exemplary only, and that from the functional descriptions given herein it will be apparent to those skilled in the art that various logic circuit implementations of each of these component elements of trellis decoder unit 250 can be employed.

The input to the BMG unit 610 is a digitized baseband data symbol stream resulting from demodulation and detection of the transmitted eight (8) level VSB signal described above with reference to the digital receiver in FIGURE 2. Each symbol in the

stream, in the ideal case of perfect transmission with no channel distortion or noise, will be at one of the eight (8) discrete levels that make up the constellation of the 8-VSB demodulator, as shown by the symbol mapper 430 in FIGURE 4. In reality, however, noise in the transmission channel affects the value of each symbol. If the noise is very low, the detected symbol value (three (3) bits) will be closer to the level of the actually transmitted symbol than to any of the other seven (7) levels, and so in principle could be obtained by simple eight (8) level slicing. If the noise level exceeds a certain value, however, the detected symbol level may be closer to an incorrect one of the eight (8) constellation values. It is under these conditions that trellis encoding, wherein the value of each encoded symbol depends on present as well as previous symbol values, achieves significant improvement of the receiver bit error rate.

FIGURE 7 illustrates a block diagram of a prior art adaptive channel equalizer 700 for use in equalizer and phase tracker unit 240. Prior art adaptive channel equalizer unit 700 comprises a forward equalizer (FE) filter 710 and a decision feedback equalizer (DFE) filter 720. The output from forward equalizer (FE) filter 710 is added to the output from decision feedback equalizer (DFE) filter 720 in adder unit 730 to form the output of adaptive channel equalizer unit 700.

Forward equalizer (FE) filter 710 accepts the uncompensated channel symbol data as its input. In contrast, decision feedback equalizer (DFE) filter 720 requires for its input an "estimate" of the symbol that was transmitted over the channel before the symbol was corrupted by noise.

As is well known, DFE filter 720 can receive an estimate of the output symbol by simply "slicing" the equalizer output. The term "slicing" refers to the process of taking the allowed symbol value (of the eight (8) levels specified by the 8-VSB ATSC Standard) that is nearest to that of the actual output. In the embodiment shown in FIGURE 7, level slicer 740 provides the "sliced" symbols to DFE filter 720 through multiplexer 750. This method of providing estimates of the output symbols to DFE filter 720 can suffer from error propagation caused by slicing errors.

As is also well known, DFE filter 720 can be adapted either in a "trained mode" or in a "blind" mode. In the "trained mode" DFE filter 720 receives a "training sequence" of known symbols (through multiplexer 750) at a certain known time. DFE filter 720 compares the known training sequence with the "equalizer error for trained adaptation." The equalizer error for trained adaptation is obtained by subtracting the equalizer output from the known training sequence. DFE filter 720 then adjusts its operation to

cause the equalizer output to match the known sequence of training signals.

Alternatively, DFE filter 720 can operate in a "blind mode." In the "blind mode" DFE filter 720 receives an "equalizer error for blind adaptation" from blind error unit 760. Blind error unit 760 compares the equalizer output with an expected statistical distribution of the data to generate the equalizer error blind adaptation. DFE filter 720 then adjusts its operation to cause the equalizer output to match the expected statistical distribution of the data.

FIGURE 8 Illustrates a conventional adaptive finite impulse response (FIR) filter 800 for use in forward equalizer (FE) filter 710 and in decision feedback equalizer (DFE) filter 720. The coefficients of FIR filter 800 are computed to compensate as much as possible for channel distortions. The length of FIR filter 800 corresponds to the maximum impairment delay that FIR filter 800 is designed to correct for.

FIR filter 800 comprises a number of filter tap cells 810 (also referred to as "filter taps"). Each filter tap 810 comprises a data storage register 820, a coefficient storage register 830, and multiplier 840. The output of multiplier 840 is input to an adder unit 850. Adder unit 850 sums all of the weighted tap values to generate a filter output. Filter tap 810 also comprises a

coefficient adaptation unit 860 that computes the updated filter coefficients. The coefficient adaptation unit 860 has the following inputs: (1) the current coefficient value, (2) the data tap value, and (3) a measure of the equalizer error (i.e., the difference between the expected signal value and the actual output signal value). The coefficient adaptation unit 860 operates only when the adaptation process is being performed.

A commonly used method of computing the filter coefficients uses the well known least mean square (LMS) algorithm. The LMS algorithm is a successive approximation technique that uses the current coefficient and data tap values as well as the equalizer error to compute the new coefficient value. The LMS algorithm repeats the procedure until each filter coefficient converges to the desired optimum value.

In a typical LMS algorithm the coefficient vector is determined using the following formula:

$$C_{n+1} = C_n + \mu E d_n \qquad (2)$$

where C_n is the coefficient vector at time n, μ is an adaptation speed constant, and d_n is the data vector in the filter at time n. E is the error calculated from the output of the equalizer. E can be calculated in a decision directed fashion using the known training sequence embedded in the data stream. Alternatively, E can be calculated in a blind fashion using a CMA algorithm.

The abbreviation CMA stands for "constant modulus algorithm."

FIGURE 9 illustrates a block diagram of the present invention showing the connection of forward equalizer (FE) filter 710 to trellis decoder 250 and the connection of trellis decoder 250 to decision feedback equalizer (DFE) filter 720. The output from forward equalizer (FE) filter 710 is added to the output from decision feedback equalizer (DFE) filter 720 in adder unit 730 to form the input to trellis decoder 250. The path memory outputs from trellis decoder 250 are fed back to decision feedback equalizer (DFE) filter 720. As will be more fully explained, information from the path memory outputs is used to reduce errors in decision feedback equalizer (DFE) filter 720.

The ATSC standard specifies a rate 1/2 code trellis decoder where the symbols are interleaved into twelve (12) different trellis decoders. The ATSC standard specifies path memory output lengths from twelve (12) symbols to sixteen (16) symbols. Thus, in presently available ATSC trellis decoder embodiments a path memory of twelve (12) to sixteen (16) delays is typically used before symbol decisions are made. When combined with the interleaving, the delay amounts to a latency of one hundred forty four (144) symbols (i.e., twelve (12) delays times twelve (12) symbols) to one hundred ninety two (192) symbols (i.e., sixteen (16) delays times twelve (12) symbols). With these latencies, the

output of the trellis decoder is of little use to the decision feedback equalizer (DFE) filter.

However, in the present invention, after each path memory stage in trellis decoder 250, a "best guess" for each symbol can be generated that will have a lower probability of error than the "hard" decisions made on the eight (8) level equalizer output. These "best guesses" can be fed back into DFE filter 720 as soon as they are available.

Trellis decoder 250 simultaneously makes available the entire traceback path for one of the twelve (12) trellis coded data streams. In every stage of the traceback memory in trellis decoder 250 a branch metric and a survivor path are available from which a symbol can be decoded. The "best guess" for each symbol can serve as an improved "estimate" for the symbol to be provided to DFE filter 720.

Therefore, when the path memory length is sixteen (16), trellis decoder 250 can provide current information concerning the most recent sixteen (16) symbols. Information concerning the first (or earliest) symbol of the set of sixteen (16) symbols will be accurate because that symbol will have been fully decoded. The current information concerning the remaining fifteen (15) symbols of the set will not be as accurate as it will become after the remaining fifteen (15) symbols are fully decoded. But the current

information concerning the remaining fifteen (15) symbols of the set will be more accurate than the information available from the "hard" slicer decisions available using prior art methods.

FIGURE 10 illustrates a block diagram showing in more detail the connection of the trellis decoder 250 to the decision feedback equalizer (DFE) filter 720. Forward equalizer (FE) filter 710 is a filter having M taps. Decision feedback equalizer (DFE) filter 720 is an equalization filter having N taps. Branch metric generator (BMG) unit 610 and add-compare-select (ACS) unit 620 of trellis decoder 250 are shown in FIGURE 10 as trellis decoder unit 1010.

As previously described, the output from forward equalizer (FE) filter 710 is added to the output from decision feedback equalizer (DFE) filter 720 in adder unit 730 to form the input to trellis decoder unit 1010. Least mean square (LMS) calculation unit 1020 also receives a copy of the input to trellis decoder unit 1010. Path memory unit (PMU) 630, traceback unit 640, and subset bit delay unit 650 are represented schematically in FIGURE 10 as consecutive stages. In particular, the stages comprise stage number one (No. 1) 1030, stage number two (No. 2) 1040, stage number three (No. 3) 1050, . . . , and stage number X (No. X) 1060. In the ATSC standard, the value X typically takes on the values twelve (12) or sixteen (16).

As shown in FIGURE 10, a path memory output from each of the

X stages is connected to a tapped delay line (TDL) of N tap DFE filter 720. Each stage provides twelve (12) symbol inputs (one symbol input for every twelve (12) symbols for the ATSC standard). Each of the tapped delay lines (TDL) is coupled to a respective multiplier having respective data tap coefficients C [0:11], C [12:23], C [24:35], . . . , C [12(X-1):N]. The outputs of the respective multipliers are summed in adder unit 1070. The output of the adder unit 1070 is fed back to adder unit 730.

In this manner, N tap DFE filter 720 receives an improved estimate or "best guess" for each symbol in the trellis decoder symbol stream. The improved estimate has a lower probability of error than the "hard" slicer decisions available using prior art methods.

FIGURE 11 illustrates a block diagram of the present invention showing a combination of a first equalizer unit 1110 and a first trellis decoder 1120 and a combination of a second equalizer unit 1140 and a second trellis decoder 1150. First equalizer unit 1110 comprises a forward equalizer (FE) and a decision feedback equalizer (DFE) of the type previously described. Second equalizer unit 1140 comprises a forward equalizer (FE) and a decision feedback equalizer (DFE) of the type previously described.

In this embodiment of the present invention, a first equalizer and trellis decoder combination is used to estimate the symbol

stream, and (2) then the received symbol stream is used in a second equalizer and trellis decoder combination. First trellis decoder 1120 operates on the output of the first equalizer unit 1110. After throughput latency of the first trellis decoder 1120 (i.e., approximately twelve (12) times the trace back depth) hard decisions are output.

In a parallel path the first equalizer unit 1110 and the first trellis decoder 1120, data is buffered in a "first in, first out" buffer 1130. Buffer 1130 compensates for the latency of the first equalizer unit 1110 and the first trellis decoder 1120. The channel distorted symbols from buffer 1130 are then fed to the second equalizer unit 1140. The adaptation of the second equalizer unit 1140 uses a different error metric than the first equalizer unit 1120. The error is calculated using the hard decisions from the first trellis decoder 1120. In this manner, the second equalizer unit 1140 can run in a data based decision directed mode.

In addition, the decision feedback equalizer (DFE) portion of the second equalizer unit 1140 can use the hard decisions from first trellis decoder 1120 as input to minimize error propagation in the second equalizer unit 1140. Further, because reliable "best guesses" are available from second trellis decoder 1150, they can be fed back into the decision feedback equalizer (DFE) portion of the second equalizer unit 1140 to further minimize error

propagation. The hard decision output of second trellis decoder 1150 is then fed to data de-interleaver 260 and then to a Reed Solomon decoder as specified in the ATSC standard.

FIGURE 12 illustrates a flow diagram showing an advantageous embodiment of the method of the present invention. The steps of the method are collectively referred to with the reference numeral 1200. Each of the X path memory unit outputs of trellis decoder 250 are connected to the inputs of X filter tap cells in DFE filter 720 (step 1210). In each stage (stage number one (No. 1) 1030, stage number two (No. 2) 1040, etc.) of path memory unit 630 of trellis decoder 250, a symbol is decoded that represents the "best guess" value for the symbol (step 1220).

Each of the X decoded "best guess" symbols is sent to the respective inputs of the X filter tap cells in DFE filter 720 (step 1230). DFE filter 720 uses the X decoded "best guess" symbol values as estimates to perform channel equalization (step 1240). The process is continued for each of the subsequent set of X symbols that appears in the path memory unit 630 of trellis decoder 250 (step 1250).

It is necessary that trellis decoder 250 be capable of providing the entire survivor path that corresponds to the current input symbol. In particular, the sequence of symbols that constitute this path will be fed back to DFE filter 720.

The sequence of symbols can be reconstructed from the state transition and uncoded bit information stored in the corresponding path memories.

FIGURE 13 illustrates a block diagram of an advantageous embodiment of the two stage equalizer 1300 of the present invention. Two stage equalizer 1300 generally comprises a first stage equalizer (EQ1) 1310 and a second stage equalizer (EQ2) 1320. First stage equalizer (EQ1) 1310 comprises a forward equalizer filter (FE1) 710, a decision feedback equalization filter (DFE1) 720, a trellis decoder 250, and an adder unit 730. Second stage equalizer (EQ2) 1320 comprises forward equalizer filter (FE2) 1350, decision feedback equalization filter (DFE2) 1340, and adder unit 1360.

Let R_k represent the input to the first stage equalizer (EQ1) 1310. Let the number (N1 + 1) be the number of taps in forward equalizer filter (FE1) 710. The filter coefficients of forward equalizer filter (FE1) 710 at time k are $f^k = \{f^k_0, f^k_1, \ldots, f^k_{N1}\}$. The output of forward equalizer filter (FE1) 710 at time k is B_k.

Similarly, let the number N2 be the number of taps in decision feedback equalization filter (DFE1) 720. The filter coefficients of decision feedback equalizer filter (DFE1) 720 at time k are $g^k = \{g^k_1, g^k_2, \ldots, g^k_{N2}\}$. Decision feedback equalization filter (DFE1) 720 is a multiple input, single output time variant filter.

The contents of the delay lines of decision feedback equalization filter (DFE1) 720 at time k are $A^k = \{A^k_1, A^k_2, \ldots, A^k_{N2}\}$. The output of first stage equalizer 1310 at time k is denoted as Y_k. The output Y_k is computed as follows:

$$Y_k = \sum_{n=0}^{N1} f^k{}_n R_{k-n} + \sum_{n=1}^{N2} g^k{}_n A^k{}_n \qquad (3)$$

Let r_k represent the input to the second stage equalizer (EQ2) 1320. Let the number (N1 + 1) be the number of taps in forward equalizer filter (FE2) 1350. The filter coefficients of forward equalizer filter (FE2) 1350 at time k are $f^k = \{f^k_0, f^k_1, \ldots, f^k_{N1}\}$. The output of forward equalizer filter (FE2) 1350 at time k is b_k.

Similarly, let the number N2 be the number of taps in decision feedback equalization filter (DFE2) 1340. The filter coefficients of decision feedback equalizer filter (DFE2) 1340 at time k are $g^k = \{g^k_1, g^k_2, \ldots, g^k_{N2}\}$.

The outputs of trellis decoder 250 at time k are $a^k = \{a^k_1, a^k_2, \ldots, a^k_{N2}\}$. The output of second stage equalizer 1320 at time k is denoted as y_k. The output y_k is computed as follows:

$$y_k = \sum_{n=0}^{N1} f^k{}_n r_{k-n} + \sum_{n=1}^{N2} g^k{}_n a_{k-n} \qquad (4)$$

Assume that X is the depth of the traceback memory of trellis

decoder 250. Further assume that M is the number of independent trellis decoder units in trellis decoder 250. For the ATSC standard, the value of M is twelve. Then, at time k, it is possible to obtain X decisions from the minimum path of the trellis decoder unit that is active at time k. The output decisions of trellis decoder 250 at time k are denoted by $v^k = \{v^k1, v^k2, \ldots, v^kX\}$. It is then apparent that

$$A^{k+1}{}_{M(I-1)+1} = v^k{}_i \quad \text{for} \quad i = 1,2,\ldots,X \tag{5}$$

$$A^{k+1}{}_n = A^k{}_{n-1} \quad \text{for} \quad n \neq M(i-1)+1 \quad [n > 1] \tag{6}$$

The input of decision feedback equalization filter (DFE2) 1340 is given by

$$a^k = v^k{}_X \tag{7}$$

From this it is observed that only X locations in the feedback path of decision feedback equalization filter (DFE1) 720 need to be replaced with v^k. When decision feedback equalization filter (DFE1) 720 is configured as a standard shift register delay line, v^k corresponds to a fixed location in the delay line, thereby simplifying the implementation of the interface between trellis decoder 250 and the feedback path to decision feedback equalization filter (DFE1) 720.

For adaptive channel equalization applications, the filter taps can be updated using standard algorithms with the second stage equalizer (EQ2) 1320. For forward equalizer filter (FE2) 1350 the

updated filter taps are:

$$f_n^{k+1} = f_n^k + \mu e_k r^*_{k-n} \quad \text{for } n = 0,1,2,\ldots,N1 \qquad (8)$$

For decision feedback equalization filter (DFE2) 1340 the updated filter taps are:

$$g_n^{k+1} = g_n^k + \mu e_k a_{k-n} \quad \text{for } n = 0,1,2,\ldots,N1 \qquad (9)$$

where μ is a small constant and e_k is the error term. Note that during start-up the taps could be updated using the contents of the first stage equalizer (EQ1) 1310.

The error needed to update the taps can be obtained either from blind algorithms (e.g., constant modulus algorithm (CMA)) or from decision directed algorithms. In the case of the decision directed algorithm, the error is calculated as :

$$e_k = a_k - y_k \qquad (10)$$

The use of this expression for the error in the tap update equations requires that the decisions a_k be reliable. These decisions in two stage equalizer 1300 are obtained from trellis decoder 250 deep in the traceback memory. Thus one may be tempted to assume that these decisions will be correct. However, there is no guarantee that these decisions will be correct. When the decisions are unreliable, then the use of the decision directed tap update process will result in a performance that is worse than the performance of the blind algorithms.

In order to avoid the use of unreliable decisions in the

decision directed tap update process, a mechanism is needed to determine the reliability of the decisions. This reliability measure can be used to switch off and to switch on the decision directed tap update process.

Inspection of the structure and operation of trellis decoder 250 reveals that such a reliability measure can be extracted from the traceback memory in the following manner. When all the survivor paths of trellis decoder 250 stem from a single state, then it is most likely that the decision corresponding to this single state will be correct. This assumption in fact underlies the basic fundamental concept of the Viterbi algorithm for trellis decoders. By measuring how many survivor paths stem from a particular state under consideration, the resulting measure can be used to switch between using (1) a decision directed tap update process, (2) a blind tap update process, (3) a combination of decision directed and blind tap update processes, and (4) using no tap update process.

When switching between decision directed and blind tap update processes, one must be careful concerning the frequency of the switching. The switching between a decision directed tap update process and a blind tap update process must be carried out over a long period of time (i.e., over a large number of samples) to insure reliability. The reliability measure can be averaged over a

long period of time and the average value can be used to smoothly control the switching point between the two types of tap update processes.

Due to implementation constraints, there will be some latency in the feedback path of the first stage equalizer (EQ1) 1310. This latency is denoted by the letter d. Then Equation (2) will be modified as follows:

$$Y_k = \sum_{n=0}^{N1} f^k{}_n R_{k-n} + \sum_{n=d+1}^{N2} g^k{}_n A^k{}_n \qquad (11)$$

This implies that post echoes that are d samples away from the main path will not be equalized by the feedback portion of first stage equalizer (EQ1) 1310, but rather by the forward equalizer portion (i.e., forward equalizer filter (FE1) 710). In the conventional equalizer case, these echoes will be equalized by the linear equalizer. Because typical indoor channels have strong echo components near the main path, these echoes in the conventional case may stress the linear equalizer.

In the two stage equalizer 1300 of the present invention, the second stage equalizer (EQ2) 1320 will not have any latency limitation because (unlike first stage equalizer (EQ1) 1310) it does not comprise a true feedback system. Such post echoes could thus conveniently be handled by the second stage equalizer (EQ2) 1320. Nevertheless, if the input from trellis decoder 250 has a

strong echo component, trellis decoder 250 may not produce reliable decisions.

Because second stage equalizer (EQ2) 1320 is based on a forward system, a similar argument may be extended to the cancellation of pre-echoes (i.e., echoes that appear before the main path) using second stage equalizer (EQ2) 1320. The cancellation of pre-echoes may be achieved by suitably choosing the delay D in "first in, first out" buffer 1330 and by appropriate computations in decision feedback equalization filter (DFE2) 1340. The delay D represents the delay between the R_k signal (the input to first stage equalizer (EQ1) 1310) and the r_k signal (the input to second stage equalizer (EQ2) 1320).

Assuming that the input to decision feedback equalization filter (DFE2) 1340 (i.e., a_k) is quasi error free, it is tempting to assume that the pre-echoes can be cancelled by second stage equalizer (EQ2) 1320. However, the primary condition for the a_k signals to be quasi error free is the cancellation of pre-echoes by first stage equalizer (EQ1) 1310. If first stage equalizer (EQ1) 1310 does not adequately remove pre-echoes, then it will be difficult for trellis decoder 250 to produce correct decisions.

FIGURE 14 illustrates a block diagram of a two stage equalizer 1400 having less complexity than the two stage equalizer 1300 shown in FIGURE 13. The form of two stage equalizer 1400 is based on the

assumption that the forward filter coefficients f^k remain constant for the duration of D symbols. This assumption is valid for a relatively small value of D with respect to the dynamics of the channel. Under this assumption, it is reasonable to assume that the output, B_k, of forward equalizer filter (FE1) 710 and the output, b_k, of decision feedback equalization filter (DFE1) 720 are related by:

$$b_k = B_{k-D} \tag{12}$$

This means that a delayed output of forward equalizer filter (FE1) 710 can be substituted for the output of decision feedback equalization filter (DFE1) 720.

This arrangement is shown in FIGURE 14. R_k represents the input to forward equalizer filter (FE1) 710. The output of forward equalizer filter (FE1) 710 (i.e., signal B_k) is provided to delay buffer 1410 where the signal is delayed by D symbols. The output of delay buffer 1410 (i.e., signal b_k) is provided to adder unit 1360.

The output of trellis decoder 250 (i.e., signal a_k) is provided to decision feedback equalization filter (DFE2) 1340. The output of decision feedback equalization filter (DFE2) 1340 is combined with signal b_k in adder unit 1360 or provide the two stage equalizer output y_k.

The output of trellis decoder 250 (i.e., signal a_k) is

provided to error unit 1420. Trellis decoder 250 also sends to error unit 1420 a signal that represents the number of states identical to the state that produced a_k. This number is referred to as the "confidence" number and is represented in FIGURE 14 with the letters "CONF." The "confidence" number is averaged and the averaged result is used to control the type of error calculation. Error unit 1420 also receives output signal y_k. Error unit 1420 calculates and outputs error signal e_k. Error unit 1420 can calculate the error using either a blind error calculation algorithm or a least mean squares (LMS) calculation algorithm.

FIGURE 15 illustrates a block diagram of one advantageous embodiment of an implementation 1500 of two stage equalizer 1400. In this configuration blocks that naturally share hardware are grouped together for seamless integration of the two stage equalizer of the present invention into a compact configuration. In implementation 1500 forward equalizer filter unit 1510 has two inputs. The first input, R_k, is needed for the computation of the tap updates. The second input, r_k, is needed for the computation of the output y_k.

Decision feedback equalization filter unit 1520 has X symbol inputs 1530. The letter X represents the depth of the trellis decoder traceback memory. The two outputs of decision feedback equalization filter unit 1520 correspond to the output of decision

feedback equalization filter (DFE1) 720 and decision feedback equalization filter (DFE2) 1340.

The error is calculated in error unit 1420 and passed to forward equalizer filter unit 1510 and to decision feedback equalization filter unit 1520 for tap update. Slicer 1550 is provided to make slicer decisions. Control unit 1560 provides control signals.

Implementation 1500 requires a delay unit (within random access memory (RAM) 1540) to store the signals r_k and b_k. The signal r_k is computed from the expression:

$$r_k = R_{k-D} \tag{13}$$

The signal b_k is computed from the expression:

$$b_k = B_{k-D} \tag{14}$$

Both of the sequences, r_k and b_k, can be stored using a single read only memory (RAM) 1540.

While the present invention has been described in detail with respect to certain embodiments thereof, those skilled in the art should understand that they can make various changes, substitutions modifications, alterations, and adaptations in the present invention without departing from the concept and scope of the invention in its broadest form.